Warm-Up

CST/CAHSEE: Grade 8 Algebra I 15.0	**Review: Grade 6 AF 2.3**

Andy's driving speed for a 4-hour trip was 45 miles per hour. During his first 3 hours he drove 40 miles per hour. What was his average speed for the last hour of the trip?

A) 50 miles per hour

B) 60 miles per hour

C) 65 miles per hour

D) 70 miles per hour

Using Bar Models to Solve Rate Problems In Algebra I

Bar Models can be setup a variety of ways. Bar Models provide students with a way to approach word problems, help them define their variable and offer an alternative to the distance = rate $\times$ time formula. Ultimately, we still want students to be able to set up the equation.

Example 1: "Average Speed" Problem

You Try 1

Phil's driving speed for a 6-hour trip was 65 miles per hour. During his first 4 hours, he drove 60 miles per hour. What was his average speed for the last 2 hours of the trip?

You Try 1

Phil's driving speed for a 6-hour trip was 65 miles per hour. During his first 4 hours, he drove 60 miles per hour. What was his average speed for the last 2 hours of the trip?

BAR MODEL

Let x = the average speed for the last 2 hours
How many hours?

1st	2nd	3rd	4th	5th	6th	
65	65	65	65	65	65	= 390

Average speed

1st	2nd	3rd	4th	5th	6th
60	60	60	60	x	x

Actual speed
240 miles

So, 390 miles subtracted by 240 miles is 150 miles for the last 2 hours.

∴ the average speed for the last hour is 75 mph

Let x = the average speed for the last 2 hours

$$6(65) = 4(60) + 2(\ )$$
$$\quad 0 \quad 2\ 0 \quad 2$$
$$- \quad = \quad - \quad + \quad x$$
$$150 = 2x$$
$$\frac{150}{2} \quad \frac{2x}{2}$$
$$75 = x$$

∴ the average speed for the last 2 hours was 75 mph

Example 2: "Opposite Directions" Problem

Two airplanes left the same airport traveling in opposite directions. If one airplane averages 400 miles per hour and the other airplane averages 250 miles per hour, in how many hours will the distance between the two planes be 1625 miles?

BAR MODEL

Let x = the number of hours until the planes are 1625 miles apart

0 1 2 3 Hours

1950 miles

(Discuss how the distance each plane travels is the total distance that they are apart.)

So it takes longer than 2 hours but less than 3 hours.

0 1 2 2.5 3 Hours

0 650 1300 1625 1925 Miles

If we split the 3rd hour in half, we see that it will take 2 ! hours.

∴ It will take 2 ! hours.

Let x = the number of hours until the planes are 1625 miles apart

$x + x = 1625$

$\frac{650x}{650} = \frac{1625}{650}$

$x = 2\frac{1}{2}$

∴ It will take 2 ! hours.

OR

3 2.5

You Try 2

Two airplanes leave New York at the same time in opposite directions. If one airplane averages 300 miles per hour and the other airplane averages 200 miles per hour, in how many hours will the distance between the two planes be 2500 miles?

You Try 3

A sailboat leaves San Francisco for Los Angeles at 30 mph. A motorboat leaves the same place two hours later in San Francisco for Los Angeles at 50 mph. How long will it take until the motorboat catches up to the sailboat?

Example 4: "Meet" Problem

A car leaves San Francisco for Anaheim traveling an average of 65 mph. At the same time, another car leaves Anaheim for San Francisco traveling an average of 60 mph. If it is 500 miles between San Francisco and Anaheim, how long until the two cars meet?

BAR MODEL

Let x = the time until the two cars meet

0	1	2	3	4	Hours
65 + 60	65 + 60	65 + 60	65 + 60		
0	125	250	375	500	Total miles

(Discuss how the total distance is how much closer the cars are to each other.)

∴ It will take the cars 4 hours to meet.

Let x = the time until the two cars meet

$$65x + 60x = 500$$

$$\frac{125x}{125} = \frac{500}{125}$$

$$x = 4$$

∴ It will take the cars 4 hours to meet.

You Try 4

Anahi leaves her house for her friend's house walking at 4 mph. At the same time, her friend Jessica leaves her house for Anahi's house walking at 3 mph. If they live 21 miles apart, how long will it take until Anahi and Jessica meet?

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Anahi leaves her house for her friend's house walking at 4 mph. At the same time, her friend Jessica leaves her house for Anahi's house walking at 3 mph. If they live 21 miles apart, how long will it take until Anahi and Jessica meet?

BAR MODEL

Let x = the time until the two friends meet

0 1 2 3 Hours

3 + 4	3 + 4	3 + 4

0 7 14 21 Total miles

(Discuss how the total distance is how much closer the friends are to each other.)

∴ It will take them 3 hours to meet.

Let x = the time until the two friends meet

$4x \quad 3x \quad 21$

$7x = 21$

$\frac{x}{} = \frac{}{}$

∴ It will take them 3 hours to meet.